

# Electrostatics

$$F_e = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

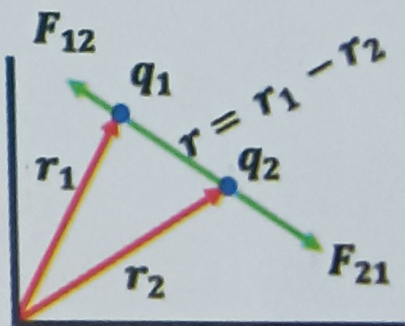
$q_1$  and  $q_2$  are charge on two bodies  
 $r$  = distance between two bodies  
 $\epsilon_0$  = permittivity of free space  
 its value is  $8.854 \times 10^{-12} \text{ C}^2/\text{Nm}^2$

## Dielectric Constant

(Relative permittivity of the medium)

$$K = \epsilon_r = \frac{\epsilon}{\epsilon_0}$$

## Vector Form of Coulomb's Law



$$\vec{F}_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12}$$

$$\vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_{21}^2} \hat{r}_{21}$$

Force between Multiple Charges

$$\vec{F}_{12} = \frac{1}{4\pi\epsilon_0} \left( \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12} + \frac{q_1 q_3}{r_{13}^2} \hat{r}_{13} + \dots + \frac{q_1 q_n}{r_{1n}^2} \hat{r}_{1n} \right)$$

# Electric Field

Electric Field Intensity

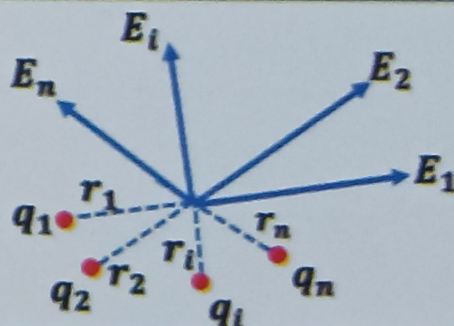
$$E = \lim_{q_0 \rightarrow 0} \frac{F}{q_0}$$

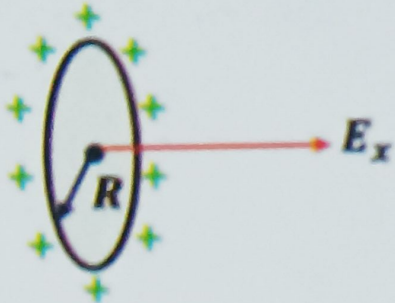
Electric Field due to a Point Charge

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

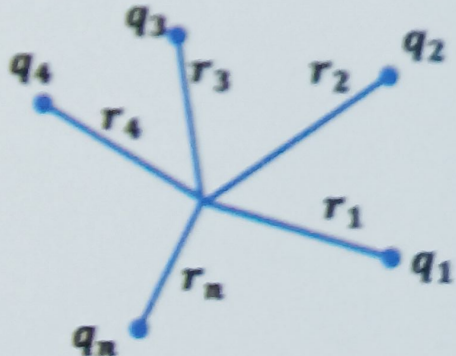
Electric Field due to System of Charges

$$E(r) = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^n \frac{q}{r_i^2} \hat{r}_i$$



<p><b>Electric field due to the line charge distribution</b></p>	$E = \frac{1}{4\pi\epsilon_0} \int_L \frac{\lambda}{r^2} dL \hat{r}$ <p><math>\lambda =</math> linear charge density</p>	
<p><b>Electric Field of a Ring of Charge</b></p> 	$E_x = \left( \frac{1}{4\pi\epsilon_0} \right) \frac{qx}{(x^2 + R^2)^{3/2}}$	
<p><math>E_x = 0</math> at <math>x = 0</math> i.e., field is zero at the centre of the ring.</p>	$E = \frac{1}{4\pi\epsilon_0} \frac{q}{x^2}$ <p>For <math>x \gg r</math></p>	$E_{max} = \frac{2}{\sqrt{3}} \left( \frac{1}{4\pi\epsilon_0} \frac{q}{R^2} \right)$

## Electric Potential

<p><b>Electric Potential</b></p>	$V = \frac{W}{q}$
<p><b>Electric Potential due to a Point Charge</b></p>	$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$
<p><b>Potential due to System of Charges</b></p> $V = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^n \frac{q_i}{r_i}$	
<p><b>Potential Gradient</b></p>	<p>Potential Gradient = <math>\frac{dV}{dr}</math></p>

### Electric Flux

$$\Delta\phi_E = E\Delta S \cos \theta$$

### Gauss's Theorem

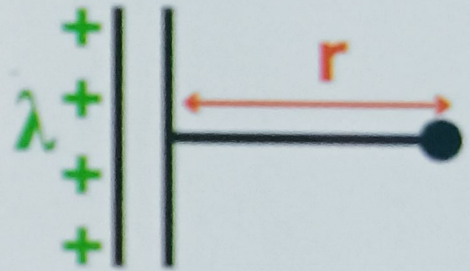
The electric flux over any enclosed surface is  $\frac{1}{\epsilon_0}$  times the total charge enclosed by the surface

$$\phi_E = \oint_S E \cdot dS = \frac{1}{\epsilon_0} \sum q$$

### Applications of Gauss's Theorem

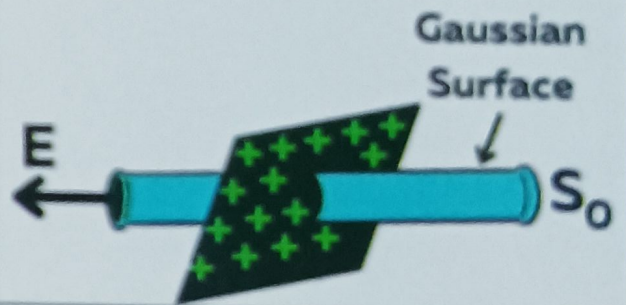
Electric Field Intensity due to an Infinite Line Charge

$$E = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{r}$$



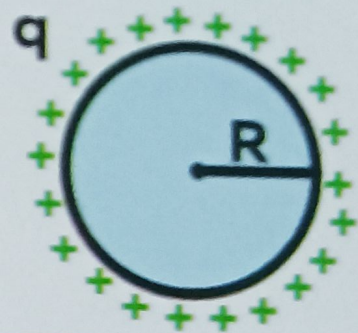
Electric Field Near an Infinite Plane Sheet of Charge

$$E = \frac{\sigma}{2\epsilon_0}$$



Electric Field outside the Charged Spherical Shell

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$



Electric Field inside the Charged Spherical Shell

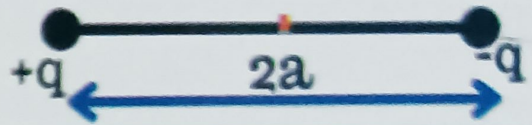
$$E = 0$$



# Electric Dipole

## Electric Dipole

Dipole Moment,  $p = q \times 2a$

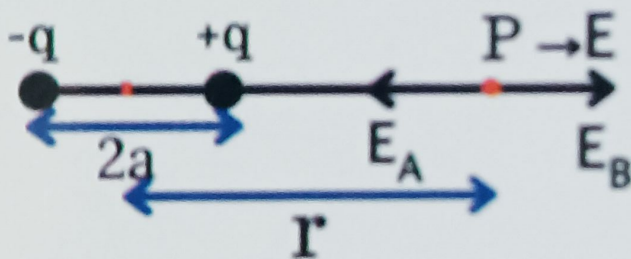


## Electric Field Intensity and Potential due to an Electric Dipole

### On Axial Line

$$E = \frac{1}{4\pi\epsilon_0} \frac{2pr}{(r^2 - a^2)^2}$$

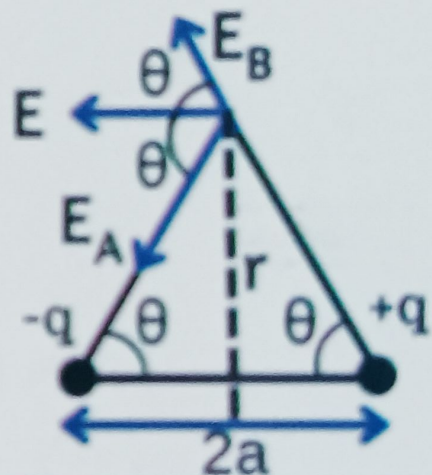
$$V = \frac{1}{4\pi\epsilon_0} \frac{p}{(r^2 - a^2)}$$



### On Equatorial line

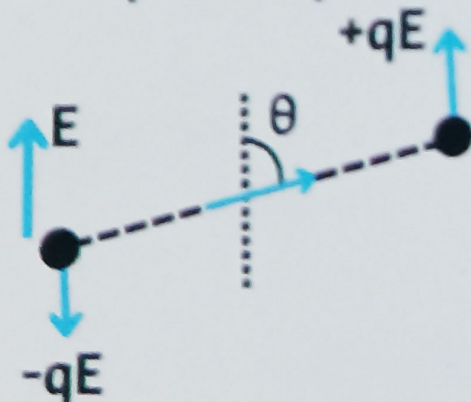
$$E_x = \frac{1}{4\pi\epsilon_0} \frac{p}{(r^2 + a^2)^{3/2}}$$

$$V = 0$$



### Torque on Dipole in a Uniform External Field

$$\tau = Ep \sin \theta = p \times E$$



### Potential Energy of a Dipole in a Uniform Electric Field

$$W = pE(\cos \theta_1 - \cos \theta_2)$$

$$\text{If, } \theta_1 = 90^\circ \text{ \& } \theta_2 = \theta$$

$$W = pE(\cos 90^\circ - \cos \theta) = -pE \cos \theta = -p \cdot E$$

# Capacitor

Capacitance of a Conductor

$$C = \frac{q}{V}$$

Capacitance of an Isolated Spherical Conductor

$$C = 4\pi\epsilon_0 R$$

## Parallel Plate Capacitor

Electric Field

$$E = \frac{\sigma}{\epsilon_0}$$

Electric potential

$$\Delta V = \frac{q}{A\epsilon_0} d$$

Capacitance

$$C = \frac{KA\epsilon_0}{d}$$

For air  $K = 1$

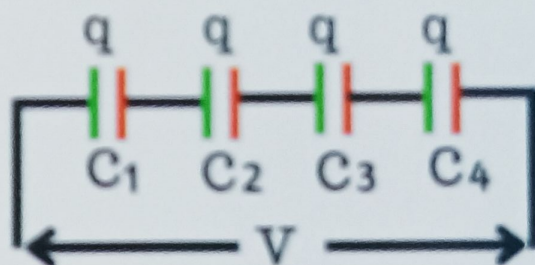
## Combination of Capacitors

In Series

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} \dots$$

For Different Potential Differences

$$V = V_1 + V_2 + V_3 \dots$$

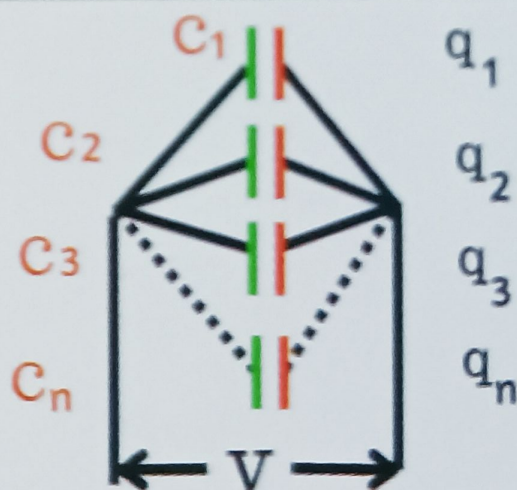


In Parallel

$$C = C_1 + C_2 + C_3 \dots$$

Total Charge on Capacitors

$$q = q_1 + q_2 + q_3 \dots$$

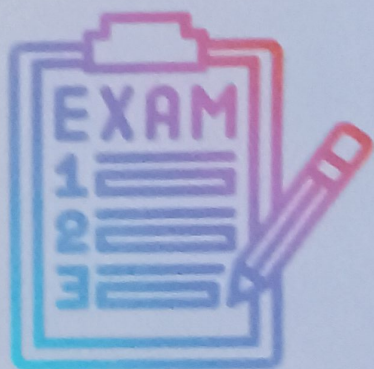
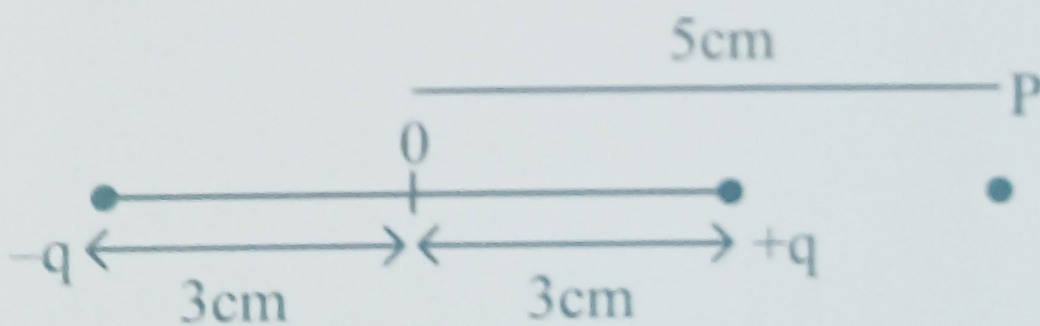


Potential Energy Stored in a Capacitor

$$U = \frac{1}{2} CV^2 = \frac{1}{2} \frac{q^2}{C}$$

## NEET 2023 PYQ'S (Chapter 14-15)

- The ratio of frequencies of fundamental harmonic produced by an open pipe to that of closed pipe having the same length is **2:1**
- An electric dipole is placed at an angle of  $30^\circ$  with an electric field of intensity  $2 \times 10^5 \text{ NC}^{-1}$ . It experiences a torque equal to 4 Nm. Calculate the magnitude of charge on the dipole, if the dipole length is 2 cm: **2mC**
- if  $\oint \vec{E} \cdot d\vec{S} = 0$  over a surface is 0, then : **the number of flux lines entering the surface must be equal to the number of flux lines leaving it**
- An electric dipole is placed as shown in the figure. The electric potential (in  $10^2 \text{ V}$ ) at point P due to the dipole is  **$(3/8)qK$**



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